

Tipping point analysis of atmospheric oxygen concentration

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APO meeting, 19th September 2015

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- Interface between business, academia and government
- Science with impact: ensure that measurements are comparable and traceable to the same standard units of the System International (SI)
- 700 staff





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Energy







Tipping points:



bifurcations and transitions in time series

changes in system states



Tipping point toolbox (being developed since 2007)



- Anticipating (pre-tipping): early warning signals of tipping points
- Detecting (tipping): potential analysis
- Forecasting (post-tipping): PDF & potential analysis, recently added bayesian techniques

AD with four potentials





Potential contour plot at different time scales

We generate artificial data using Euler scheme

$$x_{t+\Delta t} \approx x_t - \frac{dU}{dx}\Big|_t \cdot \Delta t + (W_{t+\Delta t} - W_t)$$

W is a Wiener process

Potentials:

$$U(z) = z^{2}$$

$$U(z) = z^{4} - 2z^{2}$$

$$U(z) = z^{6} - 4.5z^{4} + 5z^{2}$$

$$U(z) = z^{8} - 6.5z^{6} + 13z^{4} - 8z^{2}$$



Atmospheric oxygen concentration

Paper: V.Livina, T.Vaz, A.Forbes, Chaos, 2015

Atmospheric oxygen raw data





Unit is the change of $\frac{0_2}{N_2}$ ratio in *per meg*, 0.0001% of decline of oxygen concentration, reference is based on tanks of air pumped in the mid-1980s stored in the US lab





Data = global trend + seasonality + fluctuations

What kind of trend?

Is seasonality stable?

Are fluctuations stable?

Synchrosqueezing: wavelet-based seasonal trend





Detrended data: fluctuations





Early warning indicators





Potential analysis





Information criteria for model fit of annually averaged data



Likely:



Seasonality is stable

Fluctuations are stable

Trend is parabolic

Projection of oxygen decline





Uncertainties: modelling and technological

Resources utilisation (World Bank)





Global GHG emissions





Hydrogen cars: dual-fuel BMW 7



Two fuel tanks

170 litres of liquid hydrogen:driving range 200 km;73 litres of petrol:driving range 480 km

This technology uses about 2.7 times less volume of oxygen for combustion in hydrogen mode than in petrol mode.

Most of modern hydrogen generation is not green! (steam reforming of hydrocarbons at high temperature; also hydrolysis) 20



Technology with double sink of oxygen



Even when oil and gas will not be used for energy, they will be used for materials synthesis

Possible collaboration in a publishing project



- To engage experts from various fields: geochemistry, physiology, wildfires and combustion
- To assess the oxygen decline time scale and impact

"The future of the atmospheric oxygen" ?



- Measurement techniques and standardisation
- Derivation of long-term trend of oxygen from GCMs (100-200 years)
- Physiological impact of oxygen decline
- Long-term projections of oxygen under various scenarios of demographics and consumption development
- Assessment of impact of modern industrial technologies
- Raising social awareness of the oxygen decline



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The idea needs communal effort and support!



Thank you

Early warning signal model





Livina & Lenton, GRL 2007

Series is approximated by an AR(1) process, and exponential decay of the autocorrelation function (ACF) is estimated. Thus ACF-indicator c is defined; its gradual trend towards value 1 indicates critical behaviour.

 $y_{n+1} = cy_n + \sigma \eta_n,$ $c = \exp(-\kappa \Delta t), \kappa \text{ is decay rate}$ $(\kappa = 0 \text{ when } c = 1)$

Artificial data with increasing memory Livina et al, Physica A, 2012





When ACF-indicator reaches critical value 1, DFA-indicator is still capable to reflect the variability in the variance

Potential analysis model



$$\dot{z}(t) = -U'(z) + \sigma\eta$$
$$U(z) = a_4 z^4 + a_3 z^3 + a_2 z^2 + a_1 z$$



double-well potential

Kwasniok & Lohmann, Phys Rev E, 2009 Livina et al, Climate of the Past 2010

PotentialvsProbability Density Function (PDF)



Fokker-Planck equation

$$\partial_t p(z,t) = \partial_z [U'(z)p(z,t)] + \frac{1}{2}\sigma^2 \partial_z^2 p(z,t)$$
$$p(z) \approx \exp[-2U(z)/\sigma^2]$$

If we assume that the considered subset of data is stationary, then

$$U = -\frac{\sigma^2}{2} \log p_d$$

bimodal histogram

double-well potential

GRIP & NGRIP temperature proxies NPL



(Livina et al, Climate of the past, 2010) $\operatorname{Physical Laboratory}$ (Livina et al, Climate of the past, 2010) $\operatorname{Physical Laboratory}$ $\operatorname{Physical Laboratory}$ $\operatorname{Physic$

Calcium data: bifurcation at 27-28 kyr BP



Potential forecast algorithm



Livina et al, Physica A 2013

- Collect coefficients of Chebyshev approximation of PDF in sliding windows
- Extrapolate series of the coefficients
- Reconstruct forecast PDF
- Simulate time series from the obtained PDF (rejection sampling)
- Sort the series according to historic data (taking into account seasonality)

Oxygen period of observations is short, horizon forecast long: other techniques are necessary